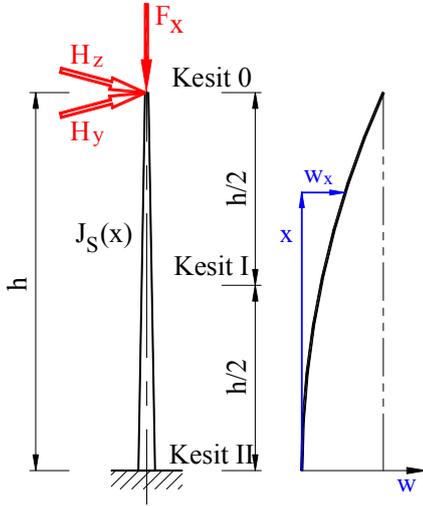
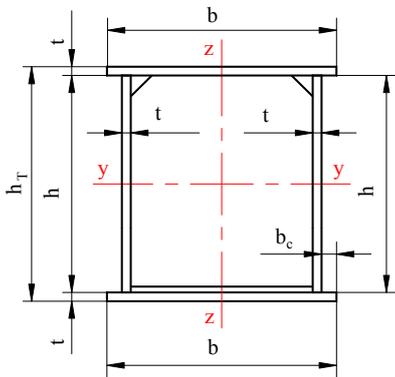


Zorlama: Eksenel kuvvet ve iki eksenli eğilme momenti.

Bilinen değerler:



Resim 1



Resim 2

Kesit II, alt 4 m:

Faktörler

$x := 4 \cdot m$

Malzeme := "S235" $f_y := 235 \cdot MPa$ $E := 210000 \cdot MPa$
 $\gamma_M := 1.1$ $h_S := 4 \cdot m$

Emniyetli akma mukavemeti $f_{EM} := \frac{f_y}{\gamma_M}$ $f_{EM} = 213.6 \cdot MPa$

$F_x := 700 \cdot kN$

Kabul: Eğrinin şekli parabol

$H_y := 60 \cdot kN$

$H_z := 40 \cdot kN$

Kesit 0, üst 0 m:

$b_0 := 420 \cdot mm$

$h_0 := 380 \cdot mm$

$t := 10 \cdot mm$

$b_c := 10 \cdot mm$

$h_{T0} := h_0 + 2 \cdot t$ $h_{T0} = 400 \cdot mm$ $z_0 := 0.5 \cdot (h_0 + t)$ $z_0 = 195 \cdot mm$

$$J_{y0} := 2 \cdot \frac{b_0 \cdot t^3}{12} + 2 \cdot \frac{t \cdot h_0^3}{12} + 2 \cdot t \cdot b_0 \cdot z_0^2$$

$J_{y0} = 410.9 \cdot 10^6 \cdot mm^4$

$$W_{y0} := \frac{2 \cdot J_{y0}}{h_{T0}}$$

$W_{y0} = 2054.7 \cdot 10^3 \cdot mm^3$

$$EJ_{y0} := E \cdot J_{y0}$$

$EJ_{y0} = 86.3 \cdot MN \cdot m^2$

$$A_0 := 2 \cdot t \cdot (b_0 + h_0)$$

$A_0 = 16000 \cdot mm^2$

$$y_0 := 0.5 \cdot (b_0 + t) - b_c$$

$y_0 = 205 \cdot mm$

$$J_{z0} := 2 \cdot \frac{b_0^3 \cdot t}{12} + 2 \cdot \frac{t^3 \cdot h_0}{12} + 2 \cdot t \cdot h_0 \cdot y_0^2$$

$J_{z0} = 442.9 \cdot 10^6 \cdot mm^4$

$$W_{z0} := \frac{2 \cdot J_{z0}}{b_0}$$

$W_{z0} = 2109.2 \cdot 10^3 \cdot mm^3$

$$EJ_{z0} := E \cdot J_{z0}$$

$EJ_{z0} = 93 \cdot MN \cdot m^2$

$k_{II} := 1.5$

$b_2 := k_{II} \cdot b_0$

$b_2 = 630 \cdot mm$

$h_2 := k_{II} \cdot h_0$

$h_2 = 570 \cdot mm$

$$k_{IIb} := \frac{b_2}{b_0}$$

$k_{IIb} = 1.500$

$$k_b := \frac{k_{IIb} - 1}{h_S}$$

$k_b = 0.125 \cdot m^{-1}$

$k_{bx} = 1 + k_b \cdot x$

$$k_{IIh} := \frac{h_2}{h_0}$$

$k_{IIh} = 1.500$

$$k_h := \frac{k_{IIh} - 1}{h_S}$$

$k_h = 0.125 \cdot m^{-1}$

$k_{hx} = 1 + k_h \cdot x$

$$h_{Tx} := h_0 \cdot (1 + k_h \cdot x) + 2 \cdot t$$

$h_{Tx} = 590 \cdot mm$ $z_x := 0.5 \cdot [h_0 \cdot ((1 + k_h \cdot x)) + t]$ $z_x = 290 \cdot mm$

$$J_{y2} := 2 \cdot \left[\frac{b_0 \cdot (1 + k_b \cdot x) \cdot t^3}{12} + \frac{t \cdot [h_0 \cdot (1 + k_h \cdot x)]^3}{12} + t \cdot b_0 \cdot (1 + k_b \cdot x) \cdot z_x^2 \right]$$

$J_{y2} = 1368.4 \cdot 10^6 \cdot mm^4$

$$W_{y2} := \frac{2 \cdot J_{y2}}{h_{Tx}}$$

$$W_{y2} = 4638.7 \cdot 10^3 \cdot \text{mm}^3$$

$$EJ_{y2} := E \cdot J_{y2}$$

$$EJ_{y2} = 287.4 \cdot \text{MN} \cdot \text{m}^2$$

$$y_{II} := 0.5 \cdot (b_0 + t) - b_{\zeta} \quad y_0 = 205 \cdot \text{mm}$$

$$J_{z2} := 2 \cdot \frac{b_2^3 \cdot t}{12} + 2 \cdot \frac{t^3 \cdot h_2}{12} + 2 \cdot t \cdot h_2 \cdot [0.5 \cdot (b_2 + t) - b_{\zeta}]^2$$

$$J_{z2} = 1512.4 \cdot 10^6 \cdot \text{mm}^4$$

$$W_{z2} := \frac{2 \cdot J_{z2}}{b_2}$$

$$W_{z2} = 4801.2 \cdot 10^3 \cdot \text{mm}^3$$

$$A_2 := 2 \cdot t \cdot (b_2 + h_2)$$

$$A_2 = 24000 \cdot \text{mm}^2$$

$$EJ_{z2} := E \cdot J_{z2}$$

$$EJ_{z2} = 317.6 \cdot \text{MN} \cdot \text{m}^2$$

x e bağlı Eylemsizlik ve karşı koyma momentleri ile alan formülü:

$$J_{yx} = 2 \cdot \left[\frac{b_0 \cdot (1 + k_b \cdot x) \cdot t^3}{12} + \frac{t \cdot [h_0 \cdot (1 + k_h \cdot x)]^3}{12} + t \cdot b_0 \cdot (1 + k_b \cdot x) \cdot [0.5 \cdot [h_0 \cdot (1 + k_h \cdot x)] + t]^2 \right]$$

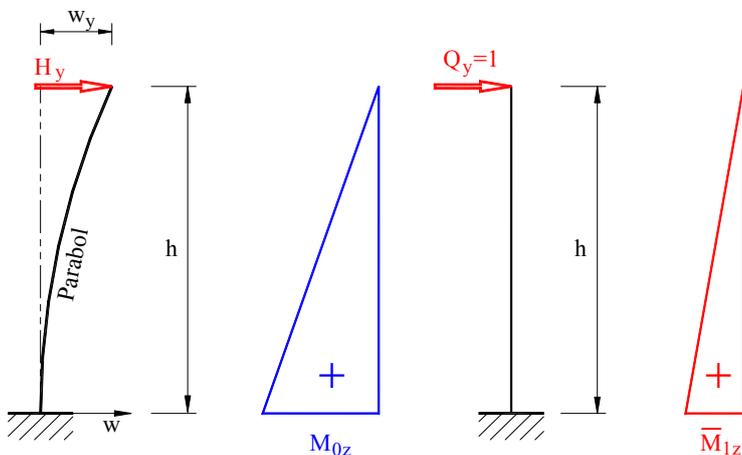
$$W_{yx} = \frac{2 \cdot J_{yx}}{h_0 \cdot (1 + k_h \cdot x) + 2 \cdot t}$$

$$J_{zx} = 2 \cdot \left[\frac{b_0^3 \cdot (1 + k_b \cdot x)^3 \cdot t}{12} + \frac{t^3 \cdot h_0 \cdot (1 + k_b \cdot x)}{12} + t \cdot h_0 \cdot (1 + k_h \cdot x) \cdot [0.5 \cdot [b_0 \cdot (1 + k_b \cdot x) - t] - b_{\zeta}]^2 \right]$$

$$W_{zx} = \frac{2 \cdot J_{zx}}{b_0 \cdot (1 + k_b \cdot x)}$$

$$A_x = 2 \cdot t \cdot [b_0 \cdot (1 + k_b \cdot x) + h_0 \cdot (1 + k_h \cdot x)]$$

Çözüm: 1. dereceli hesaplama kuralına göre



Resim 3

$$M_{0z} := H_y \cdot h_S$$

$$M_{0z} = 240 \cdot \text{kN} \cdot \text{m}$$

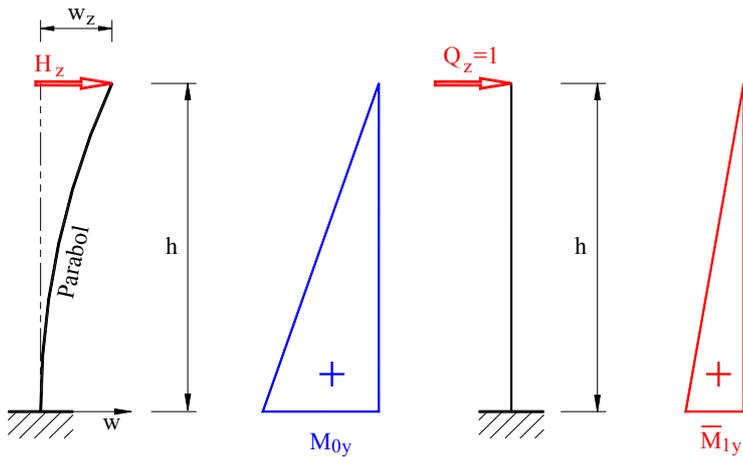
$$M_{1z} = h_S$$

$$w_{0y} = \int_0^{h_S} M_{0z} \cdot M_{1z} \cdot \frac{1}{E \cdot J_{zx}} dx$$

$$w_{0y} = \int_0^{h_S} \frac{H_y \cdot h_S^2}{E \cdot J_{zx}} dx$$

$$w_{0yx} := \int_0^{h_s} \frac{H_y \cdot h_s^2}{2 \cdot E \cdot \left[\frac{b_0 \cdot (1 + k_b \cdot x) \cdot t^3}{12} + \frac{t \cdot [h_0 \cdot (1 + k_h \cdot x)]^3}{12} + t \cdot b_0 \cdot (1 + k_b \cdot x) \cdot [0.5 \cdot [h_0 \cdot ((1 + k_h \cdot x)) + t]]^2 \right]} dx$$

$w_{0yx} = 24.876 \cdot \text{mm}$



$M_{0y} := H_z \cdot h_s$

$M_{0y} = 160 \cdot \text{kN} \cdot \text{m}$

$M_{1y} = h_s$

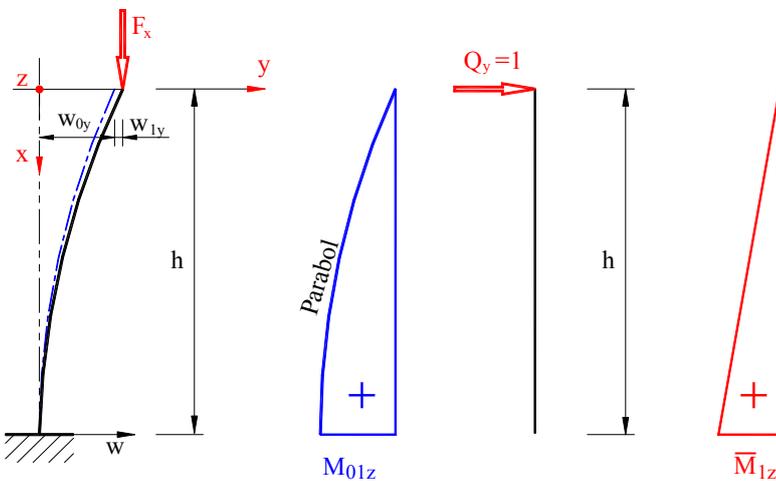
$$w_{0z} = \int_0^{h_s} M_{0y} \cdot M_{1y} \cdot \frac{1}{E J_{yx}} dx$$

$$w_{0y} = \int_0^{h_s} \frac{H_z \cdot h_s^2}{E \cdot J_{yx}} dx$$

$$w_{0zx} := \int_0^{h_s} \frac{H_z \cdot h_s^2}{2 \cdot E \cdot \left[\frac{b_0 \cdot (1 + k_b \cdot x) \cdot t^3}{12} + \frac{t \cdot [h_0 \cdot (1 + k_h \cdot x)]^3}{12} + t \cdot b_0 \cdot (1 + k_b \cdot x) \cdot [0.5 \cdot [h_0 \cdot ((1 + k_h \cdot x)) + t]]^2 \right]} dx$$

$w_{0zx} = 16.584 \cdot \text{mm}$

Vianelloya göre



Resim 5

$M_{01zx} = f(x) \cdot F_x$

$M_{1z} = x$

EJ lineer değil

$$w_{1yx} = \int_0^{h_s} M_{01zx} \cdot M_{1zx} \cdot \frac{1}{E \cdot J_{zx}} dx$$

Resim 6

Genelde parabol denklemi

$$M_{01zx} = a \cdot x^2 + b \cdot x + c$$

$$M_{01zx}(x=0) = 0$$

$$c = 0$$

$$M_{01zx}(x=h_s) = F_x \cdot w_{0max}$$

$$M_{01zx}(x=2 \cdot h_s) = 0$$

Eğer $x=2 \cdot h_s$ yerleştirilirse:

$$0 = (2 \cdot L_s)^2 a + 2 \cdot L_s \cdot b$$

$$0 = 2 \cdot L_s a + b$$

$$b = -2 \cdot a \cdot L_s$$

b yi yerleştiririm

$$x = h_s^2$$

$$M_{01zx} = a \cdot x^2 + b \cdot x + c$$

$$F_x \cdot w_0 = a \cdot h_s^2 + b \cdot h_s + 0$$

$$F_x \cdot w_0 = a \cdot h_s^2 - 2 \cdot a \cdot h_s^2$$

$$F_x \cdot w_0 = -a \cdot h_s^2$$

$$a = -\frac{F_x \cdot w_0}{h_s^2}$$

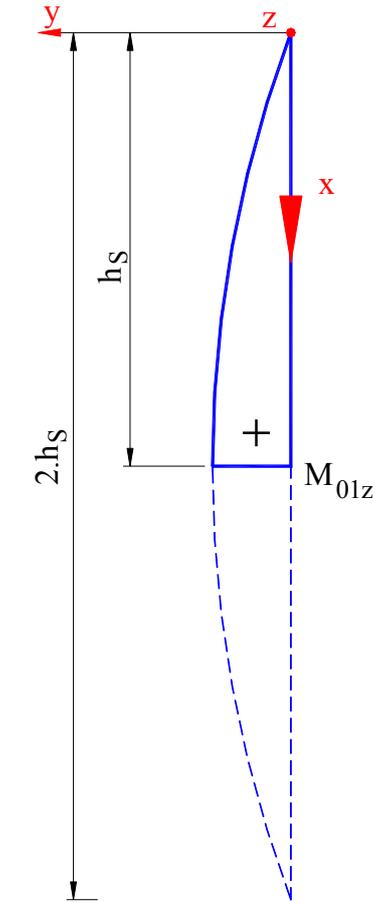
$$b = -2 \cdot a \cdot h_s$$

$$b = -\frac{2 \cdot F_x \cdot w_0}{h_s}$$

x e bağlı moment dağılımı

$$M_{01zx} = -\frac{F_x \cdot w_{0y}}{h_s^2} \cdot x^2 - \frac{2 \cdot F_x \cdot w_{0y}}{h_s} \cdot x$$

$$M_{01zx} = F_x \cdot w_{0y} \cdot \left(\frac{x^2}{h_s^2} + \frac{2 \cdot x}{h_s} \right)$$

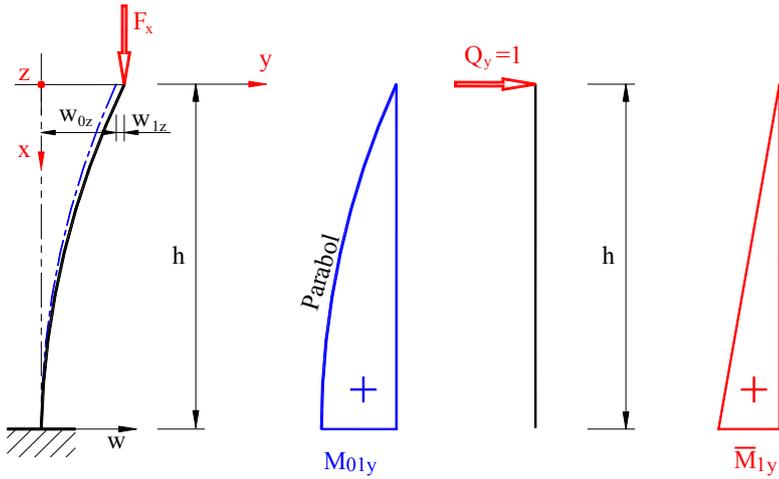


$$w_{1yx} = \int_0^{h_s} \frac{F_x \cdot w_{0y} \cdot \left(\frac{x^2}{h_s^2} + \frac{2 \cdot x}{h_s} \right) \cdot x}{2 \cdot E \cdot \left[\frac{b_0^3 \cdot (1 + k_b \cdot x)^3 \cdot t}{12} + \frac{t^3 \cdot h_0 \cdot (1 + k_b \cdot x)}{12} + t \cdot h_0 \cdot (1 + k_h \cdot x) \cdot \left[0.5 \cdot [b_0 \cdot (1 + k_b \cdot x) - t] - b_c \right]^2 \right]} dx$$

$$w_{1yx} := \int_0^{h_s} \frac{\frac{x^3}{h_s^2} + \frac{2 \cdot x^2}{h_s}}{2 \cdot E \cdot \left[\frac{b_0^3 \cdot (1 + k_b \cdot x)^3 \cdot t}{12} + \frac{t^3 \cdot h_0 \cdot (1 + k_b \cdot x)}{12} + t \cdot h_0 \cdot (1 + k_h \cdot x) \cdot \left[0.5 \cdot [b_0 \cdot (1 + k_b \cdot x) - t] - b_c \right]^2 \right]} dx$$

 $F_x \cdot w_{0y} = \text{sabit}$ İntegralin dışına alalım ve integralin değeri:

$$w_{1yx} = 64.4 \cdot \frac{10^{-9}}{N}$$



Resim 7

$$M_{01yx} = f(x) \cdot F_x$$

$$M_{1y} = x$$

EJ lineer değil

$$w_{1zx} = \int_0^{h_s} M_{01yx} \cdot M_{1yx} \cdot \frac{1}{E \cdot J_{yx}} dx$$

$$M_{01yx} = F_x \cdot w_{0z} \cdot \left(\frac{x^2}{h_s^2} + \frac{2 \cdot x}{h_s} \right)$$

$$w_{1zx} = \int_0^{h_s} \frac{F_x \cdot w_{0z} \cdot \left(\frac{x^2}{h_s^2} + \frac{2 \cdot x}{h_s} \right) \cdot x}{2 \cdot E \cdot \left[\frac{b_0 \cdot (1 + k_b \cdot x) \cdot t^3}{12} + \frac{t \cdot [h_0 \cdot (1 + k_h \cdot x)]^3}{12} + t \cdot b_0 \cdot (1 + k_b \cdot x) \cdot [0.5 \cdot [h_0 \cdot ((1 + k_h \cdot x)) + t]]^2 \right]} dx$$

$$w_{1zx} := \int_0^{h_s} \frac{\frac{x^3}{h_s^2} + \frac{2 \cdot x^2}{h_s}}{2 \cdot E \cdot \left[\frac{b_0 \cdot (1 + k_b \cdot x) \cdot t^3}{12} + \frac{t \cdot [h_0 \cdot (1 + k_h \cdot x)]^3}{12} + t \cdot b_0 \cdot (1 + k_b \cdot x) \cdot [0.5 \cdot [h_0 \cdot ((1 + k_h \cdot x)) + t]]^2 \right]} dx$$

$F_x \cdot w_{0z} = \text{sabit}$ İntegralin dışına alalım ve integralin değeri:

$$w_{1zx} = 67.2 \cdot \frac{10^{-9}}{N}$$

Kritik burkulma kuvveti

$$w_{yx} := w_{0yx} + w_{1yx} \cdot F_x \cdot w_{0yx}$$

$$w_{yx} = 26 \cdot \text{mm}$$

$$w_{zx} := w_{0zx} + w_{1zx} \cdot F_x \cdot w_{0zx}$$

$$w_{zx} = 17.4 \cdot \text{mm}$$

Eğer $F_x = F_{kr}$; $w_{y\max} = w_{0yx}$ ve $w_{z\max} = w_{0zx}$ ise:

$$w_{y\max} = F_x \cdot w_{0yx} \cdot w_{1yx} \quad 1 = F_{kry} \cdot w_{1yx}$$

$$F_{kry} := \frac{1}{w_{1yx}}$$

$$F_{kry} = 15531.5 \cdot \text{kN}$$

$$w_{z\max} = F_x \cdot w_{0zx} \cdot w_{1zx} \quad 1 = F_{krz} \cdot w_{1zx}$$

$$F_{krz} := \frac{1}{w_{1zx}}$$

$$F_{krz} = 14890 \cdot \text{kN}$$

$$F_{kr} := F_{kry}$$

$$F_{kr} = 15532 \cdot \text{kN}$$

$$F_x = 700 \cdot \text{kN}$$

Sonuç: Çubukta burkulma tehlikesi yoktur.

Kesit II de mukavemet hesabı:

Eylemsizlik radyusu	$i_{y2} := \sqrt{\frac{J_{y2}}{A_2}}$	$i_{y2} = 238.8 \cdot \text{mm}$
Euler burkulma boyu	$L_{By2} := \sqrt{\frac{EJ_{z2} \cdot \pi^2}{F_{kry}}}$	$L_{By2} = 14.206 \text{ m}$
Akma narinliđi	$\lambda_E := \pi \cdot \sqrt{\frac{E}{f_y}}$	$\lambda_E = 93.9$
Narinlik	$\lambda_{y2} := \frac{L_{By2}}{i_{y2}}$	$\lambda_{y2} = 59.5$
Bađıntılı narinlik	$\lambda_{By2} := \frac{\lambda_{y2}}{\lambda_E}$	$\lambda_{By2} = 0.634$
Merkez noktası mesafesi	$k_{ely2} := \frac{W_{y2}}{A_2}$	$k_{ely2} = 193.3 \cdot \text{mm}$
Akma kuvveti	$F_{pl2} := A_2 \cdot f_{EM}$	$F_{pl2} = 5127.3 \cdot \text{kN}$
Burkulma parametresi	$\alpha_B := 0.34$ Kaynaklı kutular her ekseninde.	
Max burkulma sehimi	$w_{y\max2} := k_{ely2} \cdot \alpha_B \cdot (\lambda_{By2} - 0.2)$	$w_{y\max2} = 28.5 \cdot \text{mm}$
Burkulma yardımcı faktörü	$\varphi_{By2} := 0.5 \cdot \left[1 + \alpha_B \cdot (\lambda_{By2} - 0.2) + \lambda_{By2}^2 \right]$	$\varphi_{By2} = 0.77$
Azaltma faktörü	$\chi_{By2} := \frac{1}{\varphi_{By2} + \sqrt{\varphi_{By2}^2 - \lambda_{By2}^2}}$	$\chi_{By2} = 0.820$
Kuvvetin mukavemet emniyeti	$S_{Fy2} := \frac{F_x}{\chi_{By2} \cdot F_{pl2}}$	$S_{Fy2} = 0.167$
Eylemsizlik radyusu	$i_{z2} := \sqrt{\frac{J_{z2}}{A_2}}$	$i_{z2} = 251 \cdot \text{mm}$
Euler burkulma boyu	$L_{Bz2} := \sqrt{\frac{EJ_{z2} \cdot \pi^2}{F_{kr}}}$	$L_{Bz2} = 14.206 \text{ m}$
Narinlik	$\lambda_{z2} := \frac{L_{Bz2}}{i_{z2}}$	$\lambda_{z2} = 56.6$
Bađıntılı narinlik	$\lambda_{Bz2} := \frac{\lambda_{z2}}{\lambda_E}$	$\lambda_{Bz2} = 0.603$
Merkez noktası mesafesi	$k_{elz2} := \frac{W_{z2}}{A_2}$	$k_{elz2} = 200.1 \cdot \text{mm}$
Max burkulma sehimi	$w_{z\max2} := k_{elz2} \cdot \alpha_B \cdot (\lambda_{Bz2} - 0.2)$	$w_{z\max2} = 27.4 \cdot \text{mm}$

Burkulma yardımcı faktörü	$\varphi_{Bz2} := 0.5 \cdot \left[1 + \alpha_B \cdot (\lambda_{Bz2} - 0.2) + \lambda_{Bz2}^2 \right]$	$\varphi_{Bz2} = 0.75$
Azaltma faktörü	$\chi_{Bz2} := \frac{1}{\varphi_{Bz2} + \sqrt{\varphi_{Bz2}^2 - \lambda_{Bz2}^2}}$	$\chi_{Bz2} = 0.836$
Kuvvetin mukavemet emniyeti	$S_{Fz2} := \frac{F_x}{\chi_{Bz2} \cdot F_{pl2}}$	$S_{Fz2} = 0.163$

Moment kontrolü:

Kesit 2 de toplam Moment	$M_{y2} := H_z \cdot h_S + F_x \cdot w_{zx}$	$M_{y2} = 172.15 \cdot \text{kN} \cdot \text{m}$
	$M_{z2} := H_y \cdot h_S + F_x \cdot w_{yx}$	$M_{z2} = 258.2 \cdot \text{kN} \cdot \text{m}$
	$M_{ply2} := W_{y2} \cdot f_{EM}$	$M_{ply2} = 991 \cdot \text{kN} \cdot \text{m}$
	$M_{plz2} := W_{z2} \cdot f_{EM}$	$M_{plz2} = 1025.7 \cdot \text{kN} \cdot \text{m}$
	$M_{yF2} := F_x \cdot w_{zx}$	$M_{yF2} = 12.2 \cdot \text{kN} \cdot \text{m}$
	$M_{zF2} := F_x \cdot w_{yx}$	$M_{zF2} = 18.2 \cdot \text{kN} \cdot \text{m}$
$\Delta M < 1$	$\Delta M_{2y} := \frac{M_{yF2}}{M_{y2}}$	$\Delta M_{2y} = 0.071$
	$\Delta M_{2z} := \frac{M_{zF2}}{M_{z2}}$	$\Delta M_{2z} = 0.070$
	$\beta_{My2} := 1.8 - 0.7 \cdot \Delta M_{2y}$	$\beta_{My2} = 1.8$
$\alpha_{pl} > 1$	$\alpha_{ply2} := \frac{M_{ply2}}{M_{y2}}$	$\alpha_{ply2} = 5.756$
$a_y \leq 0.8$	$a_{y2x} := \lambda_{By2} \cdot (2 \cdot \beta_{My2} - 4) + (\alpha_{ply2} - 1)$	$a_{y2x} = 4.44$
	$a_{y2} := \begin{cases} a_{y2x} & \text{if } a_{y2x} \leq 0.8 \\ 0.8 & \text{otherwise} \end{cases}$	$a_{y2} = 0.8$
$k_y \leq 1,5$	$k_{y2x} := 1 - \frac{F_x}{\chi_{By2} \cdot F_{pl2}} \cdot a_{y2}$	$k_{y2x} = 0.867$
	$k_{y2} := \begin{cases} k_{y2x} & \text{if } k_{y2x} \leq 1.5 \\ 1.5 & \text{otherwise} \end{cases}$	$k_{y2} = 0.867$
	$\beta_{Mz2} := 1.8 - 0.7 \cdot \Delta M_{2z}$	$\beta_{Mz2} = 1.8$
$\alpha_{pl} > 1$	$\alpha_{plz2} := \frac{M_{plz2}}{M_{z2}}$	$\alpha_{plz2} = 3.973$
	$a_{z2} := \lambda_{Bz2} \cdot (2 \cdot \beta_{Mz2} - 4) + (\alpha_{plz2} - 1)$	$a_{z2} = 2.672$
	$k_{z2} := 1 - \frac{F_x}{\chi_{Bz2} \cdot F_{pl2}} \cdot a_{z2}$	$k_{z2} = 0.564$

$$S_{2y} := \frac{F_x}{\chi_{By2} \cdot F_{pl2}} + \frac{M_{y2}}{M_{ply2}} \cdot k_{y2} + \frac{M_{z2}}{M_{plz2}} \cdot k_{z2}$$

$$S_{2y} = 0.459$$

$$S_{2z} := \frac{F_x}{\chi_{Bz2} \cdot F_{pl2}} + \frac{M_{y2}}{M_{ply2}} \cdot k_{y2} + \frac{M_{z2}}{M_{plz2}} \cdot k_{z2}$$

$$S_{2z} = 0.459$$

Sonuç: S_{2y} ve S_{2z} değerleri 1 den küçük olduğundan konstrüksiyon fonksiyonunu yapar.

Kesit I de mukavemet hesabı:

$$x1 := 2 \cdot m$$

$$y_1 := 0.5 \cdot [b_0 \cdot (1 + k_b \cdot x1) - t] - b_c$$

$$y_1 = 247.5 \cdot mm$$

$$J_{z1} := \left[2 \cdot \frac{b_0^3 \cdot (1 + k_b \cdot x1)^3 \cdot t}{12} + 2 \cdot \frac{t^3 \cdot h_0 \cdot (1 + k_h \cdot x1)}{12} + 2 \cdot t \cdot h_0 \cdot (1 + k_h \cdot x1) \cdot y_1^2 \right]$$

$$J_{z1} = 823.2 \cdot 10^6 \cdot mm^4$$

$$W_{z1} := \frac{2 \cdot J_{z1}}{b_0 \cdot (1 + k_b \cdot x1)}$$

$$W_{z1} = 3135.9 \cdot 10^3 \cdot mm^3$$

$$z_1 := 0.5 \cdot [h_0 \cdot (1 + k_h \cdot x1) + t]$$

$$z_1 = 290 \cdot mm$$

$$J_{y1} := 2 \cdot \left[\frac{b_0 \cdot (1 + k_b \cdot x1) \cdot t^3}{12} + \frac{t \cdot [h_0 \cdot (1 + k_h \cdot x1)]^3}{12} + t \cdot b_0 \cdot (1 + k_b \cdot x1) \cdot z_1^2 \right]$$

$$J_{y1} = 1368.4 \cdot 10^6 \cdot mm^4$$

$$W_{y1} := \frac{2 \cdot J_{y1}}{h_0 \cdot (1 + k_h \cdot x1) + 2 \cdot t}$$

$$W_{y1} = 5529 \cdot 10^3 \cdot mm^3$$

$$A_1 := 2 \cdot t \cdot [b_0 \cdot (1 + k_b \cdot x1) + h_0 \cdot (1 + k_h \cdot x1)]$$

$$A_1 = 20000 \cdot mm^2$$

Eylemsizlik radyusu $i_{y1} := \sqrt{\frac{J_{y1}}{A_1}}$

$$i_{y1} = 261.6 \cdot mm$$

Euler burkulma boyu $L_{By1} := \sqrt{\frac{E \cdot J_{y1} \cdot \pi^2}{F_{kry}}}$

$$L_{By1} = 13.513 \cdot m$$

Akma narinliği

$$\lambda_E = 93.9$$

Narinlik $\lambda_{y1} := \frac{L_{By1}}{i_{y1}}$

$$\lambda_{y1} = 51.7$$

Bağıntılı narinlik $\lambda_{By1} := \frac{\lambda_{y1}}{\lambda_E}$

$$\lambda_{By1} = 0.550$$

Merkez noktası mesafesi $k_{ely1} := \frac{W_{y1}}{A_1}$

$$k_{ely1} = 276.4 \cdot mm$$

Akma kuvveti $F_{pl1} := A_1 \cdot f_{EM}$

$$F_{pl1} = 4272.7 \cdot kN$$

Burkulma yardımcı faktörü	$\varphi_{By1} := 0.5 \cdot \left[1 + \alpha_B \cdot (\lambda_{By1} - 0.2) + \lambda_{By1}^2 \right]$	$\varphi_{By1} = 0.71$
Azaltma faktörü	$\chi_{By1} := \frac{1}{\varphi_{By1} + \sqrt{\varphi_{By1}^2 - \lambda_{By1}^2}}$	$\chi_{By1} = 0.861$
Kuvvetin mukavemet emniyeti	$S_{Fy1} := \frac{F_x}{\chi_{By1} \cdot F_{pl1}}$	$S_{Fy1} = 0.190$
Eylemsizlik radyusu	$i_{z1} := \sqrt{\frac{J_{z1}}{A_1}}$	$i_{z1} = 202.9 \cdot \text{mm}$
Euler burkulma boyu	$L_{Bz1} := \sqrt{\frac{E \cdot J_{z1} \cdot \pi^2}{F_{kr}}}$	$L_{Bz1} = 10.481 \text{ m}$
Narinlik	$\lambda_{z1} := \frac{L_{Bz1}}{i_{z1}}$	$\lambda_{z1} = 51.7$
Bağıntılı narinlik	$\lambda_{Bz1} := \frac{\lambda_{z1}}{\lambda_E}$	$\lambda_{Bz1} = 0.550$
Merkez noktası mesafesi	$k_{elz1} := \frac{W_{z1}}{A_1}$	$k_{elz1} = 156.8 \cdot \text{mm}$
Burkulma yardımcı faktörü	$\varphi_{Bz1} := 0.5 \cdot \left[1 + \alpha_B \cdot (\lambda_{Bz1} - 0.2) + \lambda_{Bz1}^2 \right]$	$\varphi_{Bz1} = 0.71$
Azaltma faktörü	$\chi_{Bz1} := \frac{1}{\varphi_{Bz1} + \sqrt{\varphi_{Bz1}^2 - \lambda_{Bz1}^2}}$	$\chi_{Bz1} = 0.861$
Kuvvetin mukavemet emniyeti	$S_{Fz1} := \frac{F_x}{\chi_{Bz1} \cdot F_{pl1}}$	$S_{Fz1} = 0.190$

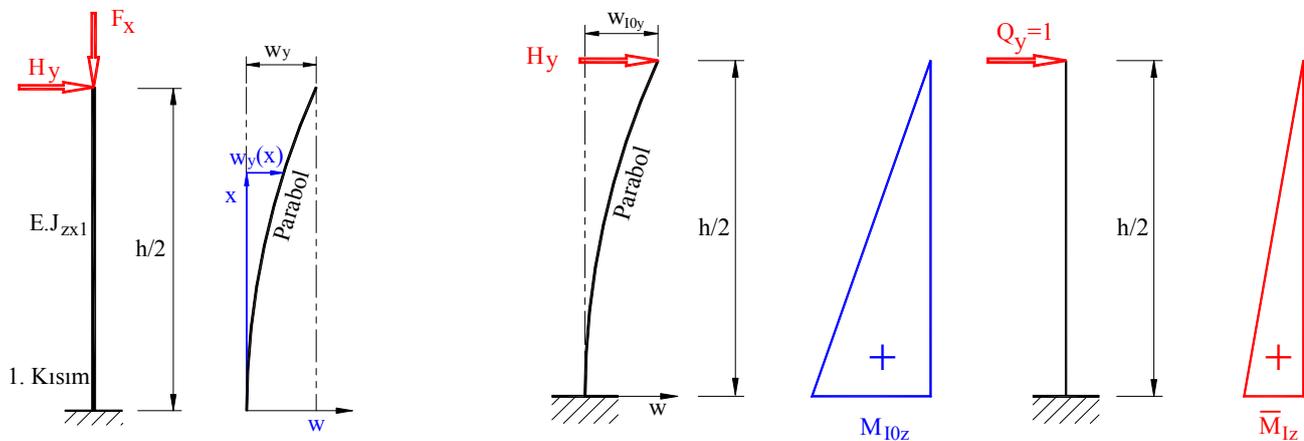
1. Kesitte burkulma tehlikesi yoktur.

1. Kesitte moment kontrolü:

$$M_{I0z} := 0.5H_y \cdot h_S$$

$$M_{I0z} = 120 \cdot \text{kN} \cdot \text{m}$$

$$M_{Iz} = 0.5 \cdot h_S$$



$$w_{10y} = \int_0^{\frac{h_S}{2}} M_{10z} \cdot M_{1z} \cdot \frac{1}{E \cdot J_{z1x}} dx$$

$$w_{10y} = \int_0^{\frac{h_S}{2}} \frac{H_y \cdot h_S}{2} \cdot \frac{h_S}{2} \cdot \frac{1}{E \cdot J_{z1x}} dx$$

$$w_{10y} = \int_0^{\frac{h_S}{2}} \frac{H_y \cdot h_S^2}{4 \cdot E \cdot J_{z1x}} dx$$

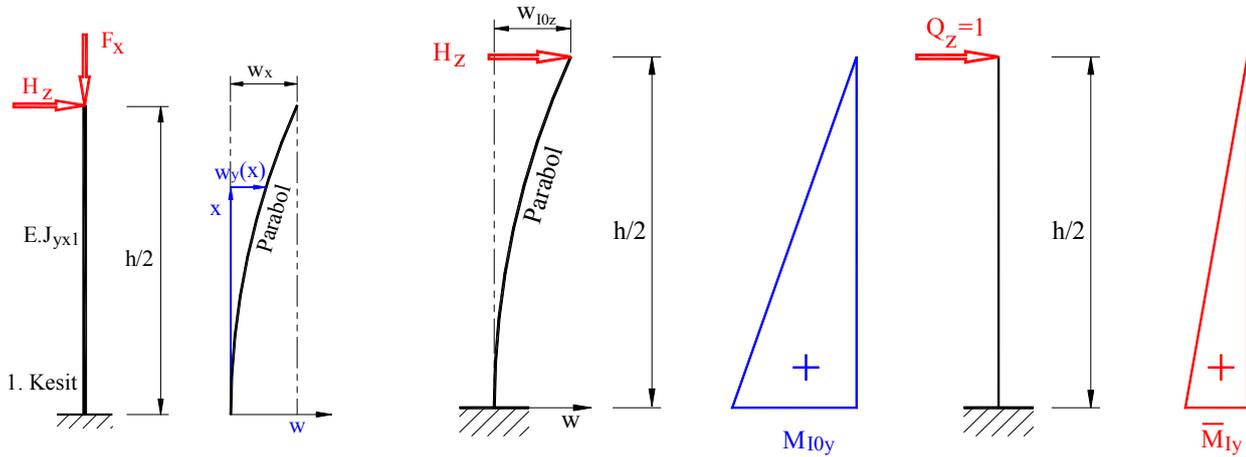
$$w_{10yx} := \int_0^{\frac{h_S}{2}} \frac{H_y \cdot h_S^2}{8 \cdot E \cdot \left[\frac{b_0^3 \cdot (1 + k_b \cdot x1)^3 \cdot t}{12} + \frac{t^3 \cdot h_0 \cdot (1 + k_h \cdot x1)}{12} + t \cdot h_0 \cdot (1 + k_h \cdot x1) \cdot [0.5 \cdot [b_0 \cdot (1 + k_b \cdot x1) - t] - b_c]^2 \right]} dx1$$

$$w_{10yx} = 3.948 \cdot \text{mm}$$

$$M_{10y} := 0.5 H_z \cdot h_S$$

$$M_{10y} = 80 \cdot \text{kN} \cdot \text{m}$$

$$M_{1y} = 0.5 \cdot h_S$$



$$w_{10z} = \int_0^{\frac{h_S}{2}} M_{10y} \cdot M_{1z} \cdot \frac{1}{E \cdot J_{y1x}} dx$$

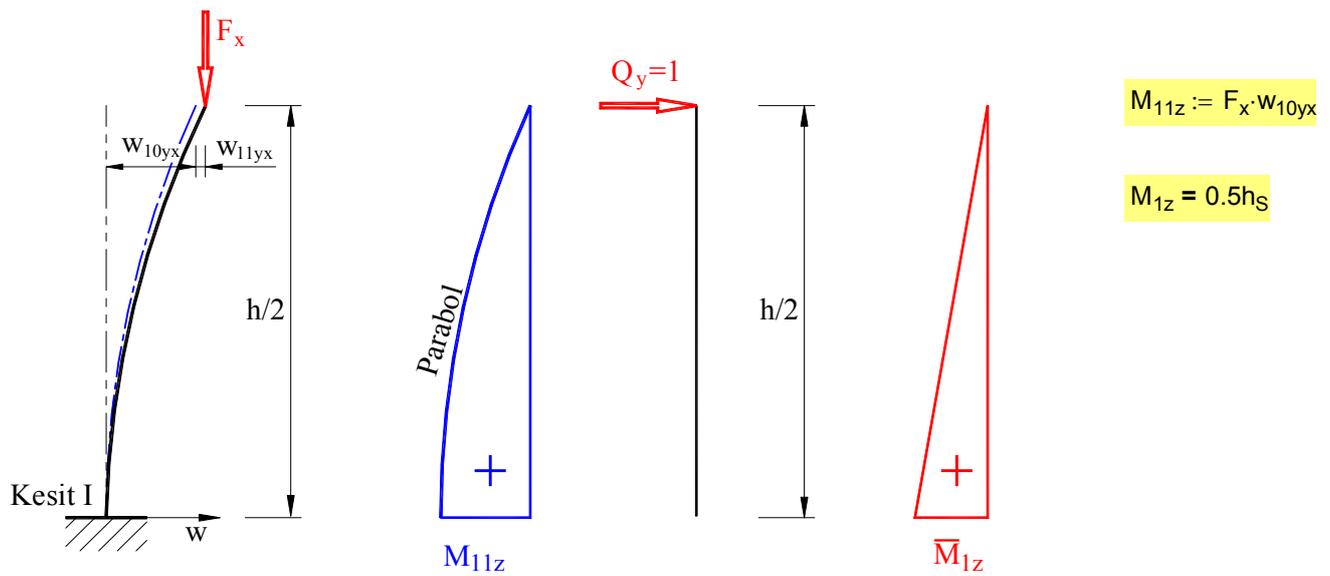
$$w_{10z} = \int_0^{\frac{h_S}{2}} \frac{H_z \cdot h_S}{2} \cdot \frac{h_S}{2} \cdot \frac{1}{E \cdot J_{y1x}} dx$$

$$w_{10z} = \int_0^{\frac{h_S}{2}} \frac{H_z \cdot h_S^2}{4 \cdot E \cdot J_{y1x}} dx$$

$$w_{10zx} := \int_0^{\frac{h_S}{2}} \frac{H_z \cdot h_S^2}{8 \cdot E \cdot \left[\frac{b_0 \cdot (1 + k_b \cdot x1) \cdot t^3}{12} + \frac{t \cdot [h_0 \cdot (1 + k_h \cdot x1)]^3}{12} + t \cdot b_0 \cdot (1 + k_b \cdot x1) \cdot [0.5 \cdot [h_0 \cdot ((1 + k_h \cdot x1)) + t]]^2 \right]} dx1$$

$$w_{10zx} = 2.680 \cdot \text{mm}$$

Vianelloya göre



$$w_{11yx} = \int_0^{\frac{h_S}{2}} M_{11z} \cdot \bar{M}_{11z} \cdot \frac{1}{EJ_{z1x}} dx$$

$$w_{11yx} = \int_0^{\frac{h_S}{2}} F_x \cdot w_{10yx} \cdot \frac{h_S}{2} \cdot \frac{1}{EJ_{z1x}} dx$$

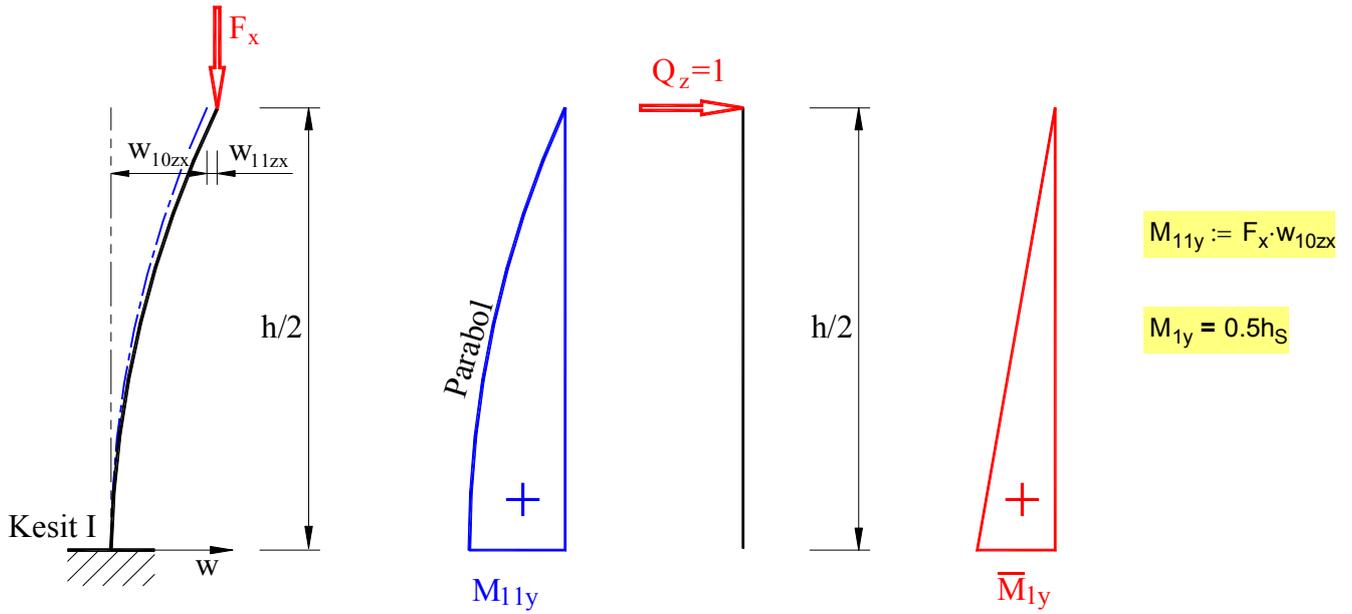
$$w_{11yx} = \int_0^{\frac{h_S}{2}} \frac{F_x \cdot w_{10yx} \cdot h_S}{2 \cdot EJ_{z1x}} dx$$

$$w_{11yx} := \int_0^{\frac{h_S}{2}} \frac{F_x \cdot w_{10yx} \cdot h_S}{4 \cdot E \cdot \left[\frac{b_0^3 \cdot (1 + k_b \cdot x_1)^3 \cdot t}{12} + \frac{t^3 \cdot h_0 \cdot (1 + k_b \cdot x_1)}{12} + t \cdot h_0 \cdot (1 + k_h \cdot x_1) \cdot \left[0.5 \cdot [b_0 \cdot (1 + k_b \cdot x_1) - t] - b_c \right]^2 \right]} dx_1$$

$$w_{11yx} = 0.091 \cdot \text{mm}$$

$$w_{12yx} := \int_0^{\frac{h_S}{2}} \frac{F_x \cdot w_{11yx} \cdot h_S}{4 \cdot E \cdot \left[\frac{b_0^3 \cdot (1 + k_b \cdot x_1)^3 \cdot t}{12} + \frac{t^3 \cdot h_0 \cdot (1 + k_b \cdot x_1)}{12} + t \cdot h_0 \cdot (1 + k_h \cdot x_1) \cdot \left[0.5 \cdot [b_0 \cdot (1 + k_b \cdot x_1) - t] - b_c \right]^2 \right]} dx_1$$

$$w_{12yx} = 0.002 \cdot \text{mm}$$



$$w_{11zx} = \int_0^{\frac{h_S}{2}} M_{11y} \cdot M_{1z} \cdot \frac{1}{EJ_{y1x}} dx \quad w_{11zx} = \int_0^{\frac{h_S}{2}} F_x \cdot w_{10zx} \cdot \frac{h_S}{2} \cdot \frac{1}{EJ_{y1x}} dx \quad w_{11yx} = \int_0^{\frac{h_S}{2}} \frac{F_x \cdot w_{10zx} \cdot h_S}{2 \cdot EJ_{y1x}} dx$$

$$w_{11zx} := \int_0^{\frac{h_S}{2}} \frac{F_x \cdot w_{10zx} \cdot h_S}{4 \cdot E \cdot \left[\frac{b_0 \cdot (1 + k_b \cdot x1) \cdot t^3}{12} + \frac{t \cdot [h_0 \cdot (1 + k_h \cdot x1)]^3}{12} + t \cdot b_0 \cdot (1 + k_b \cdot x1) \cdot [0.5 \cdot [h_0 \cdot ((1 + k_h \cdot x1)) + t]]^2 \right]} dx1$$

$$w_{11zx} = 0.063 \cdot \text{mm}$$

$$w_{12zx} := \int_0^{\frac{h_S}{2}} \frac{F_x \cdot w_{11zx} \cdot h_S}{4 \cdot E \cdot \left[\frac{b_0 \cdot (1 + k_b \cdot x1) \cdot t^3}{12} + \frac{t \cdot [h_0 \cdot (1 + k_h \cdot x1)]^3}{12} + t \cdot b_0 \cdot (1 + k_b \cdot x1) \cdot [0.5 \cdot [h_0 \cdot ((1 + k_h \cdot x1)) + t]]^2 \right]} dx1$$

$$w_{12zx} = 0.001 \cdot \text{mm}$$

Toplam sehim

$$w_{1y} := w_{10yx} + w_{11yx} + w_{12yx}$$

$$w_{1y} = 4.041 \cdot \text{mm}$$

$$w_{1z} := w_{10zx} + w_{11zx} + w_{12zx}$$

$$w_{1z} = 2.745 \cdot \text{mm}$$

Kritik burkulma kuvveti

eğer $F_x = F_{kr}$ ve $w_{10zx} = w_{11zx}$ veya $\alpha_F = \frac{w_{11zx}}{w_{10zx}} = 1$ kabul edersek:

$$1 = F_{kr1z} \cdot \int_0^{\frac{h_S}{2}} \frac{h_S}{4 \cdot E \cdot \left[\frac{b_0 \cdot (1 + k_b \cdot x_1) \cdot t^3}{12} + \frac{t \cdot [h_0 \cdot (1 + k_h \cdot x_1)]^3}{12} + t \cdot b_0 \cdot (1 + k_b \cdot x_1) \cdot [0.5 \cdot [h_0 \cdot ((1 + k_h \cdot x_1)) + t]]^2 \right]} dx_1$$

$$F_{kr1z} := \frac{1}{\int_0^{\frac{h_S}{2}} \frac{h_S}{4 \cdot E \cdot \left[\frac{b_0 \cdot (1 + k_b \cdot x_1) \cdot t^3}{12} + \frac{t \cdot [h_0 \cdot (1 + k_h \cdot x_1)]^3}{12} + t \cdot b_0 \cdot (1 + k_b \cdot x_1) \cdot [0.5 \cdot [h_0 \cdot ((1 + k_h \cdot x_1)) + t]]^2 \right]} dx_1}$$

$$F_{kr1z} = 29848 \cdot \text{kN}$$

$$1 = F_{kr1y} \cdot \int_0^{\frac{h_S}{2}} \frac{h_S}{4 \cdot E \cdot \left[\frac{b_0^3 \cdot (1 + k_b \cdot x_1)^3 \cdot t}{12} + \frac{t^3 \cdot h_0 \cdot (1 + k_b \cdot x_1)}{12} + t \cdot h_0 \cdot (1 + k_h \cdot x_1) \cdot [0.5 \cdot [b_0 \cdot (1 + k_b \cdot x_1) - t] - b_c]^2 \right]} dx_1$$

$$F_{kr1y} := \frac{1}{\int_0^{\frac{h_S}{2}} \frac{h_S}{4 \cdot E \cdot \left[\frac{b_0^3 \cdot (1 + k_b \cdot x_1)^3 \cdot t}{12} + \frac{t^3 \cdot h_0 \cdot (1 + k_b \cdot x_1)}{12} + t \cdot h_0 \cdot (1 + k_h \cdot x_1) \cdot [0.5 \cdot [b_0 \cdot (1 + k_b \cdot x_1) - t] - b_c]^2 \right]} dx_1}$$

$$F_{kr1y} = 30392.3 \cdot \text{kN}$$

$$F_{kr1} := F_{kr1z}$$

$$F_{kr1} = 29848 \cdot \text{kN}$$

$$F_x = 700 \cdot \text{kN}$$

Sonuç: Çubuğun 1. kesiti için burkulma tehlikesi yoktur.

1. Kesitte mukavemet hesabı

Moment:

$$M_{ply1} := W_{y1} \cdot f_{EM}$$

$$M_{ply1} = 1181.2 \cdot \text{kN} \cdot \text{m}$$

$$M_{plz1} := W_{z1} \cdot f_{EM}$$

$$M_{plz1} = 670 \cdot \text{kN} \cdot \text{m}$$

$$M_{y1} := H_z \cdot h_S + F_x \cdot w_{1z}$$

$$M_{y1} = 161.9 \cdot \text{kN} \cdot \text{m}$$

$$M_{z1} := H_y \cdot h_S + F_x \cdot w_{1y}$$

$$M_{z1} = 242.8 \cdot \text{kN} \cdot \text{m}$$

$$M_{y1F} := F_x \cdot w_{1z}$$

$$M_{y1F} = 1.9 \cdot \text{kN} \cdot \text{m}$$

$$M_{z1F} := F_x \cdot w_{1y}$$

$$M_{z1F} = 2.8 \cdot \text{kN} \cdot \text{m}$$

$$\Delta M < 1 \quad \Delta M_{y1} := \frac{M_{y1}}{M_{ply1}} \quad \Delta M_{y1} = 0.137$$

$$\Delta M_{z1} := \frac{M_{z1}}{M_{plz1}} \quad \Delta M_{z1} = 0.362$$

$$\beta_{My1} := 1.8 - 0.7 \cdot \Delta M_{y1} \quad \beta_{My1} = 1.7$$

$$\alpha_{pl} > 1 \quad \alpha_{ply1} := \frac{M_{ply1}}{M_{y1}} \quad \alpha_{ply1} = 7.295$$

$$a_{y1x} := \lambda_{By1} \cdot (2 \cdot \beta_{My1} - 4) + (\alpha_{ply1} - 1) \quad a_{y1x} = 5.969$$

$$a_y \leq 0.8 \quad a_{y1} := \begin{cases} a_{y1x} & \text{if } a_{y1x} \leq 0.8 \\ 0.8 & \text{otherwise} \end{cases} \quad a_{y1} = 0.8$$

$$k_{y1x} := 1 - \frac{F_x}{\chi_{By1} \cdot F_{pl1}} \cdot a_{y1} \quad k_{y1x} = 0.848$$

$$k_y \leq 1,5 \quad k_{y1} := \begin{cases} k_{y1x} & \text{if } k_{y1x} \leq 1.5 \\ 1.5 & \text{otherwise} \end{cases} \quad k_{y1} = 0.848$$

$$\beta_{Mz1} := 1.8 - 0.7 \cdot \Delta M_{z1} \quad \beta_{Mz1} = 1.5$$

$$\alpha_{pl} > 1 \quad \alpha_{plz1} := \frac{M_{plz1}}{M_{z1}} \quad \alpha_{plz1} = 2.759$$

$$a_{z1x} := \lambda_{Bz1} \cdot (2 \cdot \beta_{Mz1} - 4) + (\alpha_{plz1} - 1) \quad a_{z1x} = 1.26$$

$$a_z \leq 0.8 \quad a_{z1} := \begin{cases} a_{z1x} & \text{if } a_{z1x} \leq 0.8 \\ 0.8 & \text{otherwise} \end{cases} \quad a_{z1} = 0.8$$

$$k_{z1x} := 1 - \frac{F_x}{\chi_{Bz1} \cdot F_{pl1}} \cdot a_{z1} \quad k_{z1x} = 0.848$$

$$k_z \leq 1,5 \quad k_{z1} := \begin{cases} k_{z1x} & \text{if } k_{z1x} \leq 1.5 \\ 1.5 & \text{otherwise} \end{cases} \quad k_{z1} = 0.848$$

$$S_{y1} := \frac{F_x}{\chi_{By1} \cdot F_{pl1}} + \frac{M_{y1}}{M_{ply1}} \cdot k_{y1} + \frac{M_{z1}}{M_{plz1}} \cdot k_{z1} \quad S_{y1} = 0.614$$

$$S_{z1} := \frac{F_x}{\chi_{Bz1} \cdot F_{pl1}} + \frac{M_{y1}}{M_{ply1}} \cdot k_{y1} + \frac{M_{z1}}{M_{plz1}} \cdot k_{z1} \quad S_{z1} = 0.614$$

Sonuç: S_{Iy} ve S_{Iz} değerleri 1 den küçük olduğundan konstrüksiyon fonksiyonunu yapar.

SON
